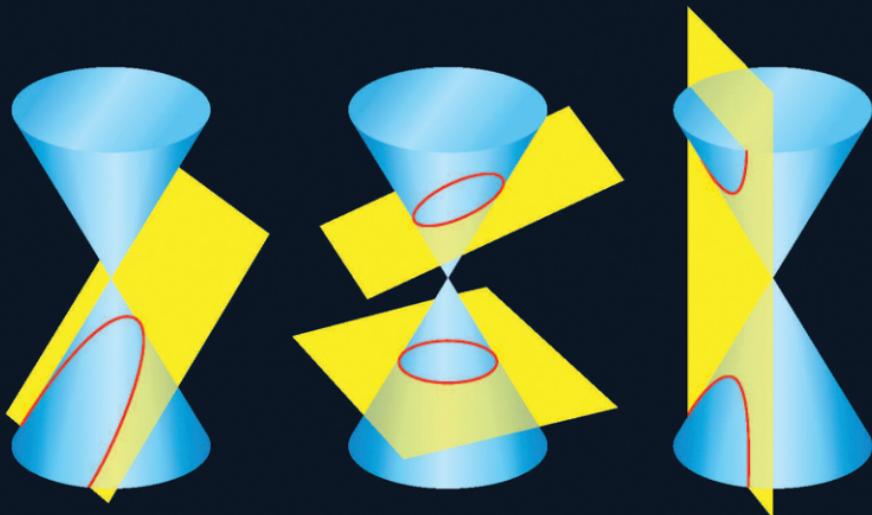


# MATH

W Charles Paulsen

# Anxiety Relief for Nearly Everyone



$$Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$$

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